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DEFECTS ASSOCIATED WITH SOLIDIFICATION OF MELT-PROCESSED SUPERALLOYS FOR THE AEROSPACE INDUSTRY FA9550-05-1-0089

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Abstract

This Materials Engineering for Affordable New Systems (MEANS) program focused on developing an integrated computational framework for predicting the conditions under which turbine blades can be produced that are free of deleterious solidification defects. To achieve this ambitious goal we studied the solidification process over length scales from subnanometer to millimeter and produced a fundamental experimental and theoretical framework for defect prediction. The present work aims at producing a fundamental predictive theory in the presence of these effects and testing this criterion experimentally. A criterion for the onset of channels, freckles, and freckle chains in nickel-base superalloys relevant to the aerospace industry has been developed by Davis and Voorhees. This criterion involves the Rayleigh number that measures buoyancy in the mushy layer versus the dissipative effects of heat conduction and viscous stresses, as well as a second parameter the Biot number that measures the lateral heat loss and hence the curvature of the interface. The segregation coefficients and density parameters of multicomponent superalloys were calculated using hybrid *ab-initio*/computational-thermodynamics modeling by Asta and Woodward. The permeability of dendritic arrays in superalloys has been determined using three-dimensional reconstructions of the solid-liquid mush and finite-element fluid simulations by Pollock and Spowart.

Close interaction with industry ensured that computational models were developed in a form that is usable in their efforts to design new alloys and processing routes. Given the broad research focus of the project the MEANS team was composed of engineers and scientists from government laboratories, industry, and universities and is diverse in its research expertise. The motivation for this research and a summary of results from the University of Michigan effort are given below.

Motivation

Preventing the formation of freckles and/or misoriented grains is important to the manufacturing and performance of single crystal superalloy components. These defects are the result of solute-induced

convective instabilities that occur at the solid-liquid interface during directional solidification [1-4]. The two most common defects observed are isolated, individual high-angle mis-oriented grains and freckle-chains. Although a number of factors have been identified as contributors to the formation of these defects, including; cooling rates, refractory alloy content and casting size and geometry [3-7], convective flow during solidification is regarded as the precursor event [8-12]. As a result, the most widely used criteria for the prediction of these defects generally consider the ratio of the buoyant to frictional forces, an interaction chiefly quantified by the Rayleigh number [10, 13-17]. Such a prediction requires not only knowledge of the fluid-flow conditions in the melt but also a detailed understanding of the geometrical domain in which the melt flows. Unfortunately, a definitive understanding of fluid flow at the scale of directionally solidified dendritic structures is still lacking. This is partly due to the many factors governing flow at this level that are both dynamic and difficult to quantify. These factors, often captured in the Rayleigh parameter R_a , Eq. (1), include composition, segregation behavior, permeability, and flow channel geometry:

$$R_a = \frac{\left(\frac{\Delta \rho}{\rho_0}\right) g \overline{K} L}{\alpha v} \tag{1}$$

where $\Delta \rho/\rho_0$ is the density gradient in the liquid, g is acceleration due to gravity, K is permeability, L is the height of the mushy zone or relative length scale and αv is the product of thermal diffusivity and kinematic viscosity [15]. Alloy chemistry influences the Rayleigh number by means of its inherent effect on the density gradient, diffusivity and viscosity. Permeability however, is dependent upon the dendritic environment through which fluid flow occurs. This research focuses on the development of three-dimensional reconstruction and characterization techniques for dendritic structures that can be used to more accurately quantify the fluid flow environment and consequently provide a more precise approximation of permeability within the dendritic array.

Experimental Procedures

Using an ALD Vacuum Technologies, Inc. Furnace (see Fig. 1), 4 kg ingots were directionally solidified in conventional Bridgman mode at the University of Michigan. The alloy used in this study is the commercial superalloy René N4 with a nominal composition of 4.2Al-0.05C-7.5Co-9.8Cr-0.15Hf-1.5Mo-0.5Nb-4.8Ta-3.5Ti-6.0W-Ni (*wt%*) and solidus and liquidus temperatures of 1300°C and 1345°C respectively. A withdrawal rate of 2.5 mm/min and thermal gradient of 40°C/cm was used. During withdrawal, the investment mold was fractured to evacuate molten liquid from the solidified dendritic structure while leaving the solid structure at the solidification front undisturbed.

Following solidification, a cast elongated plate with a cross-sectional area normal to the growth direction of 11.5 x 3 cm was produced and samples of approximately 1cm x 1cm x 1cm were removed from the solid-liquid interface of the casting with slow speed milling saws while exercising care to leave the dendritic front undisturbed. Samples were then vacuum impregnated with Buehler EpoHeat epoxy. Next, using the prototype RoboMET.3D serial sectioning system at Wright-Patterson Air Force Base, (see Fig. 2) mechanical polishing, cleaning and imaging at intervals of 2.2 µm through the sample thickness permitted acquisition of a 3-D dataset. Images were taken parallel to the primary growth direction consisting of an 8-image montage. Each image was taken at 10X with a standard resolution of 0.52 µm/pixel. Full details of the RoboMET.3D system have been previously discussed in the literature [18-20].

After a comprehensive data set was obtained, image segmentation was performed using ITT Visual Information Solutions' Interactive Data Language (IDL) along with Adobe Photoshop to render each

slice a cleaned, binary image properly aligned for stacking. Using IDL, datasets were converted to three- dimensional arrays, for visualization and evaluation of the dendritic structure at the solidification front.

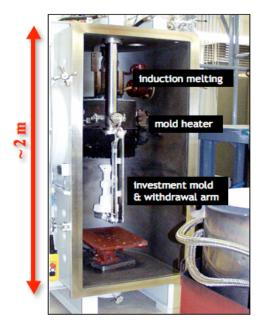


Figure 1: ALD Vacuum Technologies, Inc. Bridgman directional solidification furnace with liquid metal cooling (LMC) capability.



Figure 2: RoboMET.3D automated serial sectioning system with ALLIED metallographic polisher, robotic arm, ultrasonic cleaner and Axiovert Zeiss Inverter Microscope.

Lastly, the three-dimensional arrays were cropped for regions of liquid connectivity and surface meshes were generated using MIMICS software by Materialise followed by volume meshes that were created in GAMBIT by ANSYS. After satisfactory meshing of the interdendritic liquid was accomplished, global smoothing of the structures was introduced to diminish the pronounced tertiary dendritic features and limit flow interaction to the primary and secondary dendrite arms to ensure convergence. FLUENT was used to simulate fluid flow through the dendritic structure in the following manner. A direction of flow is assumed and a pressure gradient is imposed on the structure. Boundary conditions of zero pressure at the outlet and a flow velocity of $100\mu\text{m/sec}$ at the inlet with 'no-slip' at the walls was assumed, and interdendritic fluid flow was assumed as steady state. Using Darcy's Law, Eq. (2), permeability in these structures can be calculated as a result of the pressure change. Q is volumetric flow rate, K represents permeability whereas A accounts for cross-sectional area and L is the length over which fluid travels

between the pressure difference. Values for viscosity (μ) and density (ρ) of the molten fluid during simulation have been approximated from calculations and predictions in the literature [21, 22].

$$Q = KA \frac{\Delta P}{\mu L} \tag{2}$$

Results

The reconstruction is composed of 727 individual slices comprising a total of 12.6 GB of image information in its raw form. The removal rate for serial sectioning is shown in Figure 3, where the nominal sectioning thickness is shown as 2.2 µm per slice.

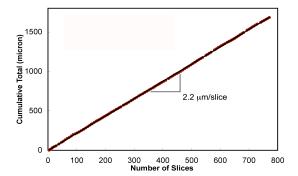


Figure 3: Serial-Sectioning Recession Rate with RoboMET.3D showing material removal as a function of slice quantity for the René N4 sample.

The total reconstructed volume is 2300 x 2300 x 1600 µm and is shown in Figure 4. Figures 5 and 6 are transverse and longitudinal slices through the dataset respectively, revealing the dendritic patterns present. Approximations of dendrite arm spacing were performed with the digital volume using two separate methods. For primary dendrite arm spacing (PDAS), binary images of individual planes perpendicular to the growth direction of the structure were isolated and primary dendrite cores were counted yielding PDAS measurements according to the following relation:

$$\lambda_1 = n_p^{-1/2} \tag{3}$$

where n_p represents the number of primary cores counted per cross-sectional area [23]. Using this method on a series of sections taken from this reconstruction, as shown in Fig. 5, an average PDAS of 480 μ m was estimated. Similarly, with regard to secondary dendrite arm spacing (SDAS) thin binary planes of the reconstruction parallel to the primary growth direction, as shown in Fig. 6, were isolated and an average SDAS measurement of 86 μ m was returned.

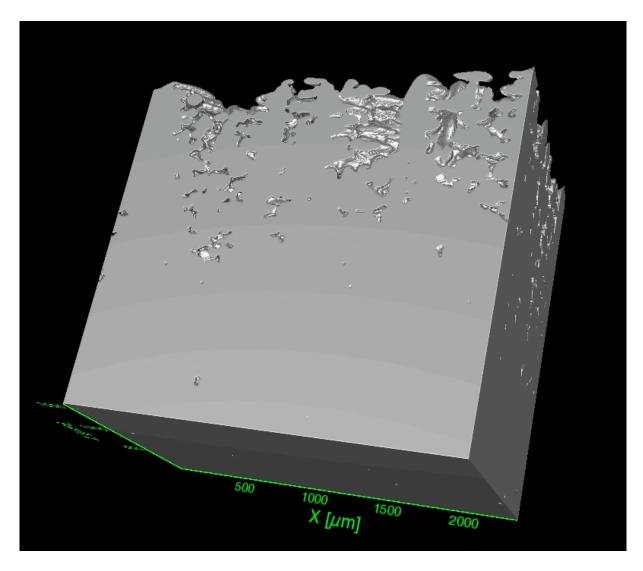


Figure 4 – Reconstructed dendritic solid-liquid interface of Rene N4, gray represents solidified superalloy, the voids represent interdendritic voids occupied by liquid prior to decanting.

Fraction Solid

By visualizing the structure as a collection of binary images, each pixel location represents either solid material or a void region formerly occupied by liquid. In this way, by summing the pixel quantities representing the presence and absence of material within successive planes along its height, the volume fraction solid (f_s) as a function of height can be measured, Figure 7. Initial inspection reveals an initially moderate decrease in solid fraction followed by a rather precipitous drop in solid fraction wherein approximately eighty percent of the volume solid decreases to zero in the upper 500 μ m of the mushy zone. This indicates a curved liquidus surface where the fraction of solid as a function of temperature varies non-linearly. There are also smaller volume fluctuations between fractions solid of $0.5 \le f_s \le 0.9$. These however, are due to locally fluctuating solid fraction caused by the presence of secondary dendrite arms.

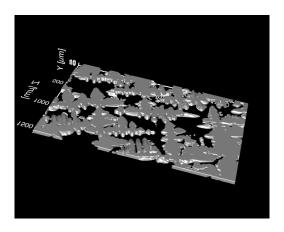


Figure 5 – Transverse cross-section of dendritic structures in which slice orientation shown is perpendicular to the primary growth direction

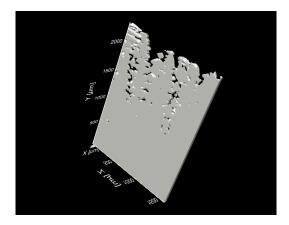


Figure 6 – Longitudinal cross-section of dendritic structures in which slice orientation shown is parallel to the primary growth direction.

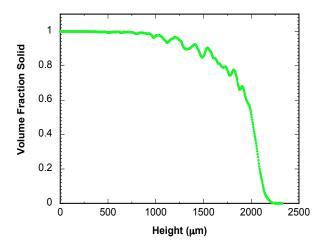


Figure 7: Volume fraction solid as a function of height in René N4 reconstructed mushy zone.

Interdendritic Channel Connectivity

For convective instabilities to develop, fluid flow through the dendritic structure must occur, making the connectivity of interdendritic channels therefore important. The channels produced by the collection of interdendritic voids throughout the mushy zone possess a high degree of connectivity, yet these channels do not unify all voids. By distinguishing each independent body of interdendritic void in the reconstruction, over 800 individual regions were identified. Importantly, 97.9% of the total voided regions are composed of a single interconnected channel. Table I summarizes the number of voids and the sum of their physical sizes for a given voxel ("volume-pixel") range. It is interesting to note that the cumulative void percentage obtained by excluding the largest eighteen independent bodies is 0.63%. The largest eighteen bodies detail the location in which molten liquid is the single or overwhelming dominant phase. The collection of remaining bodies detail encased voiding which is consistent with the level of isolated porosity, typically encountered in single crystal materials.

Table I. Interdendritic Voids: Range, Magnitudes & Overall Contribution					
Volume Threshold (μm³)	Voxel Threshold	No. of Independent Bodies	Cumulative Volume	Percentage Void	Contribution to Total
				Fraction	Voided Regions
380 700 000	10 ⁷	1	1605996489	97.9%	97.91%
38070000	10^{6}	0	0	0.00%	97.91%
3807000	10 ⁵	1	4960443	0.30%	98.21%
380700	10^{4}	16	18838565	1.15%	99.36%
38070	10^{3}	68	8238469	0.50%	99.86%
3807	10^{2}	139	1809311	0.11%	99.97%
380.7	10^{1}	273	338958	0.02%	99.99%
38.07	1	337	50027	0.00%	99.99%
*single voxel volume is 38.07 µm³					

Three-Dimensional Calculation of Flow Through Dendritic Array

For convective instabilities to develop in a dendritic structure, flow across the dendritic array normal to the solidification direction must feed the plumes that flow parallel to the solidification direction and ultimately result in freckles. Thus the influence of dendritic structure on this "cross-flow" normal to the solidification direction is of interest. A cross-sectional volume nominally 200 x 1000 x 1500 µm was selected due to its location at the dendrite tips as well its high connectivity of interdendritic regions. Surface and volume meshes of interdendritic liquid generated are shown below in Figures 8 and 9 respectively.



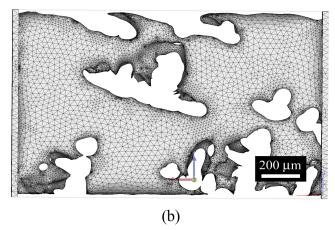


Figure 8: (a) Side view, parallel to the solidification direction and (b) Top view, normal to the solidification direction of liquid surface mesh generated with MIMICS

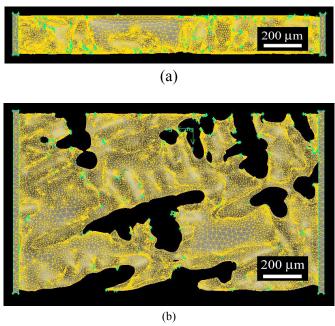


Figure 9: (a) Side view, parallel to the solidification direction and (b) Bottom view, normal to the solidification direction of liquid volume mesh generated with GAMBIT

Streamlines illustrating the flow directions in this volumetric cross-section are shown, Figure 10. Here, flow is depicted from left to right and the view presented is the orientation of the microstructure as shown in Figure 8b. In these simulations, flow is assumed as steady state and grayscale illustrates flow velocities throughout the mushy zone. It can be observed that flow velocity increases in narrow channels where flow is constricted and the flow rate must increase. Flow also seems to be dominated by the primary and secondary dendrite arms found in the central portions of the region. The pertinent range of velocity magnitudes observed range from 175 μ m/s to 3500 μ m/s. These values appear reasonable given the imposed inlet velocity of 100 μ m/s.

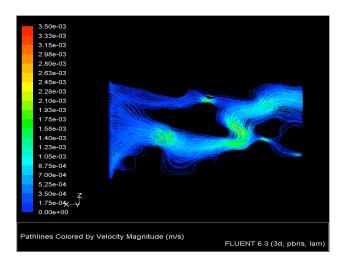


Figure 10: Streamlines of cross flow through a volumetric cross-section of the mushy zone. Solidification direction is normal to the view. Velocity magnitudes are presented in m/s.

Additionally, pressure contours throughout the structure are shown in Figure 11. Higher pressures are concentrated on the left at the velocity inlet while low pressures are present at the pressure outlet on the right. Pressure gradients are most pronounced in regions of restricted cross-section and high velocity flow. With the imposed flow and disregarding any localized fluxes at the boundary plates, a pressure differential of 14.5 Pa was measured across the structure. By measuring the local cross-section at the inlet a specific cross-sectional area and volumetric flow rate were returned. These values were then used in a formulation of Darcy's Law, Eq. (2), to derive a solution for permeability. Using this method, permeability calculated for cross-flow in this volume is 1.16 x 10⁻¹⁰ m², Calculations conducted on the flow process parallel to the primary dendrites and the growth direction showed this level of permeability was reached at a much smaller fraction liquid. Thus the secondary dendrite arm morphology and the cross-flow process are more likely to limit the onset of convective instabilities

Discussion

Primary and Secondary Dendrites

Dendrite arm spacing has often been used to not only quantify the solidification phenomena but also as an indication of casting quality in directionally solidified structures. The predominant measures are the primary and secondary dendrite arm spacings (PDAS and SDAS respectively) [24-32]. It has been well documented that fundamental relationships exist between dendrite arm spacings and casting parameters of growth rate (V) and thermal gradient (G). As such, with knowledge of G and V, an expected morphology and dendritic spacing can be approximated. While variations in the general form of the relationship exist

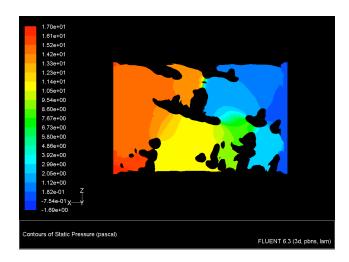


Figure 11: Pressure contours across the reconstructed liquid as a result of cross-flow. An inlet pressure of 17 Pa is present at the inlet.

[33, 34], Hunt proposed the following widely accepted relationship for primary dendrite arm spacing (λ_1) as a function of G and V [35].

$$\lambda_{1} \propto G^{-\frac{1}{2}} * V^{-\frac{1}{4}} \tag{4}$$

While PDAS can be influenced largely by the solidification front curvature and degree of lateral heat extraction, SDAS has been shown to vary fairly consistently with local solidification time according to the following behavior [36, 37]:

$$\lambda_2 \propto (G * V)^{-1/3} \tag{5}$$

Figures 12 and 13 show the dependence of PDAS and SDAS as a function of G and V, Eqs. (4) and (5), measured by Elliott et al. [5] using molds instrumented with thermocouples for verification of experimental thermal gradient. The data were generated using a set of similar withdrawal rate experiments performed in the University of Michigan's Bridgman furnace with and without liquid-Sn assisted cooling [38]. The largest deviations from Eq. 4 occur when there is large-scale transverse dendritic growth. The extent of transverse dendritic growth in the present experiments was extremely limited.

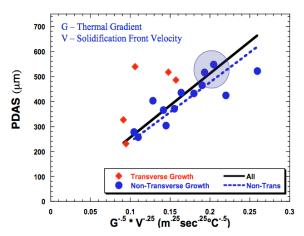


Figure 12: Measured Primary Dendrite Arm spacing plotted as a function of the product of G^{-.5} * V^{-.25}

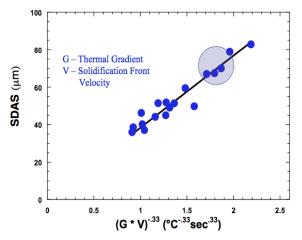


Figure 13: Measured Secondary Dendrite Arm spacing plotted as a function of the product of $(G*V)^{-33}$

Using the results in Figs. 12 and 13, local 3-D and further global 2-D PDAS and SDAS measurements were evaluated for comparison. Based on the relationships shown in Eqs. (4) and (5) and taking into account the thermal gradient (G), and solidification front velocity (V), used to produce this casting of René N4, we would expect PDAS in the range of 450-600 μm and an SDAS in the range of 60-80 μm as highlighted in Figs 12 and 13. Using 2-D metallography on material taken near the vicinity of the reconstruction, the average PDAS was measured as 560 μm whereas SDAS expressed an average measure of 82 μm .

Similarly, by using planar sections of the reconstruction, with a smaller overall cross-section compared to the 2-D measurements, the PDAS was approximated as 480 μ m and SDAS was approximated at 86 μ m, which is near the range expected. Table II summarizes these results.

Table II. Comparison of Arm Spacing Measures by Technique

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	PDAS	SDAS			
G & V Calculation	450 - 600	60 - 80			
2 – D Measurement	560	82			
3 – D Measurement	480	86			

While the 2-D measures compare well with the 3-D measures, the 3-D approximations for PDAS appear to slightly underestimate the 2-D measures due to a smaller cross-section sampled. Using 2-D measures, 1,460 dendrite cores were counted for PDAS whereas for SDAS, a portion of these cores were sectioned and 31 independent measures were taken. Given the limitation of the reconstruction, 255 dendrite cores were counted from within planes of the reconstruction to get the 3-D PDAS approximation whereas 6 representative SDAS measurements were taken by sampling through the volume.

Implications of Volume Fraction Gradient and Voiding

With a constant temperature gradient and uniform withdrawal rate, a resultant linear variation in fraction solid as a function of distance from the dendrite tips into the solid was not observed for René N4. While the literature has suggested steep declines in the volume fraction solid over the length of the mushy zone, [33, 39] here we have developed an experimental technique to directly measure this critical feature of the mushy zone. Taking the measured volume fraction solid as a function of height in the mushy zone, see Figure 7, over the first 1700 µm a decrease of approximately 0.01% fraction solid per µm is apparent while over the final 500 µm a decrease of 0.16% fraction solid per µm exists. These large-scale gradients in fraction solid will strongly influence fluid flow within the mushy zone. Permeability is highly sensitive to volume fraction, and as such, drastic changes in volume would suggest drastic fluctuations in permeability over the same length scale. Unfortunately, most solidification analyses tend to take an average volume fraction over the mush or consider shorter heights throughout the mushy zone to be reasonably free from large-scale volume fluctuations and associated large-scale fluctuations in permeability [13, 15]. In the 3-D dataset presented, over 95% of the total voids identified are united with the uppermost body, satisfying a necessary condition for convective flow and solidified material transport. However, this arrangement does not necessarily establish a sufficient condition for convective flow as the limiting flow step for such an event has been proposed as cross-flow parallel to the growth direction of the secondary dendrites [40, 41]. While further investigation of mean path diameter, length and volume of these channels is in progress, initial observation of the largest single body connected to the region of superheated liquid reveals an interesting feature. The mushy zone, as illustrated in Figure 4, extends over a height of roughly 1875 µm. The height of the largest interconnected body is approximately 900 µm. This would suggest that the potential for convective flow exists as far as halfway down into the mushy zone.

Permeability

The above Navier-Stokes fluid flow simulation suggests we can successfully calculate permeability in these structures based upon the pressure differential. It should be noted that the reconstructed liquid used in the fluid flow model shown in this work does exhibit a high volume fraction liquid (f_L) gradient over its 200 μ m height (roughly $0.4 \le f_L \le 0.7$). As such, the region of higher volume fraction likely dominates the flow calculations derived here. Nonetheless a degree of agreement exists between similar treatments of cross-flow permeability in the literature. Bhat et. al derived a dimensionless value for permeability in

cross-flow through dendritic structures [42] as a function of liquid fraction denoted by g_L . This was accomplished by dividing permeability by the square of the PDAS. By employing this convention, we arrive at a value for dimensionless permeability in this structure $K' = K/\lambda_1^2$ equal to 3.68×10^{-4} . While this value is near the range of those reported by Bhat and Porier [42, 43], their treatments suggest dimensionless permeability values in the range of $10^2 - 10^{-3}$ for liquid volume fractions in the range of 0.4 to 0.7. However, it should also be noted, their treatments report findings primarily in the Pb-Sn system with remarkably lower PDAS. The techniques for permeability analysis presented here will now permit future assessments of the influence of dendritic microstructure on fluid flow and defect formation.

Conclusions

- The primary and secondary dendritic arm spacings of the reconstruction are consistent with two-dimensional measures and are within the range of expected values based upon withdrawal rates and thermal gradients.
- For the commercial alloy René N4, volume fraction solid as a function of height does not vary linearly with the temperature gradient as might be expected. This strongly affects the permeability as a function of depth throughout the mushy zone and particularly in the upper 25%.
- At the solid-liquid solidification front, as observed in the 3-D reconstruction, the connectivity of the uppermost body of interdendritic liquid during solidification contains over ninety percent of the total interdendritic liquid and extends down through nearly half of the entire mushy zone height.
- Permeability within these structures can be calculated based upon the observed pressure differential resulting from fluid flow. The associated permeability values calculated offer reasonable agreement with similar treatments of permeability in the literature.
- Cross-flow transverse to the primary dendrites is much more restricted that the flow parallel to the growth direction.

References

- 1. S. M. Copley, A. F. Giamei, S. M. Johnson, & M. F. Hornbecker, "The Origin of Freckles in Unidirectionally Solidified Castings," *Metall. Trans*, 1 (A) (1970), 2193-2204.
- 2. A. F. Giamei & B. H. Kear, "On the Nature of Freckles in Nickel Base Superalloys," *Metall. Trans*, 1 (A) (1970), 2185-2192.
- 3. T. M. Pollock, "The growth and elevated temperature stability of high refractory nickel-base single crystals," *Materials Science and Engineering B*, B32 (1995), 255-266.

- 4. T. M. Pollock & W. H. Murphy, "The Breakdown of Single-Crystal Solidification in High Refractory Nickel-Base Alloys," *Metall. Mater. Trans. A*, 27A (4) (1996), 1081-1094.
- 5. A. J. Elliott, S. Tin, W. T. King, S. C. Huang, M. F. X. Gigliotti, & T. M. Pollock, "Directional Solidification of Large Superalloy Castings with Radiation and Liquid-Metal Cooling: A Comparative Assessment," *Metall. Mater. Trans. A*, 35A (2004), 3221-3231.
- 6. F. Scheppe, I. Wagner, & P. R. Sahm, "Advancement of the Directional Solidification Process of a Ni-Al-W Alloy" (Paper presented at the Mat. Res. Soc. Symp, Boston, MA, 2001), N.5.7.1-6
- 7. S. Tin, "Carbon Additions and Grain Defect Formation In Directionally Solidified Nickel-Base Superalloys," *University of Michigan, Ph.D. Thesis,* (2001), 1-155.
- 8. J. C. Heinrich, S. Felicelli, P. Nandapurkar, & D. R. Poirier, "Thermosolutal Convection during Dendritic Solidification of Alloys: Part II. Nonlinear Convection," *Metall. Trans. B*, 20B (1989), 883-891.
- 9. S. Motakef, "Interference of Buoyancy-Induced Convection with Segregation During Directional Solidification: Scaling Laws," *J. Crystal Growth*, 102 (1990), 197-213.
- 10. G. Muller, G. Neumann, & H. Matz, "A Two-Rayleigh Number Model of Buoyancy-Driven Convection in Vertical Melt Growth Configurations," *J. Crystal Growth*, 84 (1987), 36-49.
- 11. S. Tin & T. M. Pollock, "Stabilization of Thermosolutal Convective Instabilities in Ni-Based Single-Crystal Superalloys: Carbide Precipitation and Rayleigh Numbers," *Metall. Mater. Trans. A*, 34A (2003), 1953-1967.
- 12. S. Tin, T. M. Pollock, & W. Murphy, "Stabilization of Thermosolutal Convective Instabillities in Ni-Based Single-Crystal Superalloys: Carbon Additions and Freckle Formation," *Metall. Mater. Trans. A*, 32A (2001), 1743-1753.
- 13. C. Beckermann, J. P. Gu, & W. J. Boettinger, "Development of a Freckle Predictor via Rayleigh Number Method for Single-Crystal Nickel-Base Superalloy Casting," *Metall. Mater. Trans. A*, 31A (10) (2000), 2545-2557.
- 14. D. A. Nield, "The Thermohaline Rayleigh-Jeffreys Problem," *J. Fluid Mech*, 29 (3) (1967), 545-558.
- 15. J. C. Ramirez & C. Beckermann, "Evaluation of a Rayleigh-Number-Based Freckle Criterion for Pb-Sn Alloys and Ni-Base Superalloys," *Metall. Mater. Trans. A*, 34A (7) (2003), 1525-1536.
- 16. S. Tin & T. M. Pollock, "Predicting Freckle Formation in Single Crystal Ni-Base Superalloy," *Journal of Materials Science*, 39 (2004), 7199-7205.

- 17. M. G. Worster, "Instabilities of the Liquid and Mushy Regions During Solidification of Alloys," *J. Fluid Mech*, 237 (1992), 649-669.
- 18. B. Maruyama, J. E. Spowart, D. J. Hooper, H. M. Mullens, A. M. Druma, C. Druma, et al., "A new technique for obtaining three-dimensional structures in pitch-based carbon foams," *Scripta Materialia*, 54 (2006), 1709-1713.
- 19. J. E. Spowart, "Automated serial sectioning for 3-D analysis of microstructures," *Scripta Materialia*, 55 (2006), 5-10.
- 20. J. E. Spowart, H. M. Mullens, & B. T. Puchala, "Collecting and Analyzing Microstructures in Three Dimensions: A Fully Automated Approach," *Journal of Materials*, 55 (10) (2003), 35-37.
- 21. F. J. Cherne III & P. A. Deymier, "Calculation of Viscosity of Liquid Nickel by Molecular Dynamics Methods," *Acta Materialia*, 39 (11) (1998), 1613-1616.
- 22. K. Mukai, Z. Li, & K. C. Mills, "Prediction of the Densities of Liquid Ni-Based Superalloys," *Metall. Mater. Trans. B*, 36B (2005), 255-262.
- 23. D. G. McCartney & J. D. Hunt, "Measurements of Cell and Primary Dendrite Arm Spacings in Directionally Solidified Aluminum Allloys," *Acta Metallurgica*, 29 (1981), 1851-1863.
- 24. A. M. Glenn, S. P. Russo, & P. J. K. Paterson, "The Effect of Grain Refining on Macrosegregation and Dendrite Arm Spacing of Direct Chill Cast AA5182," *Metall. Mater. Trans. A*, 34A (2003), 1513-1523.
- 25. R. N. Grugel & Y. Zhou, "Primary Dendrite Spacing and the Effect of Off-Axis Heat Flow," *Metall. Mater. Trans. A*, 20A (1989), 969-973.
- 26. S. C. Huang & M. E. Glicksman, "Fundamentals of Dendritic Solidification-II. Development of Sidebranch Structure," *Acta Metallurgica*, 29 (1981), 717-734.
- 27. C. M. Klaren, J. D. Verhoeven, & R. Trivedi, "Primary Dendrite Spacing of Lead Dendrites in Pb-Sn and Pb-Au Alloys," *Metall. Mater. Trans. A*, 11A (11) (1980), 1853-1861.
- 28. W. Kurz & D. J. Fisher, "Dendrite Growth at the Limit of Stability: Tip Radius and Spacing," *Acta Metallurgica*, 29 (1981), 11-20.
- 29. L. Makkon, "Primary dendrite spacing in constrained solidification," *Materials Science and Engineering A*, A148 (1991), 141-143.
- 30. W. R. Osorio, P. R. Goulart, G. A. Santos, C. Moura Neto, & A. Garcia, "Effect of Dendrite Arm Spacing on Mechanical Properties and Corrosion Resistance of Al 9 Wt Pct Si

- and Zn 27 Wt Pct Al Alloys," *Metallurgical and Materials Transactions A*, 37A (8) (2006), 2525-2538.
- 31. R. Trivedi, "Interdendritic Spacing: Part II. A Comparison of Theory and Experiment," *Metall. Trans. A*, 15A (1984), 977-982.
- 32. M. Vijayakumar & S. N. Tewari, "Dendrite spacings in directionally solidified superalloy PWA-1480," *Materials Science and Engineering A*, A132 (1991), 195-201.
- 33. M. C. Flemings, "Solidification of Castings and Ingots," *Solidification Processing*, ed. (New York, NY: McGraw-Hill, Inc, 1974), 146-154
- 34. W. Kurz & D. J. Fisher, "Solidification Microstructure: Cells and Dendrites," *Fundamentals of Solidification*, ed. (Enfield, NH: Trans Tech Publications, 1998), 80-87
- 35. J. D. Hunt, "Cellular and Primary Dendrite Arm Spacings," *Solidification and Casting of Metals*, ed. J. D. Hunt (London: The Metals Society, 1979), 3-9
- 36. M. C. Flemings, "Structure Control in Cast Metals," *Solidification Technology*, ed. J. J. Burke, M. C. Flemings, & A. E. Gorum (Chestnut Hill, MA: Brook Hill Publishing Company, 1974), 3-14
- 37. R. Mehrabian, "Segregation Control in Ingot Solidification," *Solidification Technology*, ed. J. J. Burke, M. C. Flemings, & A. E. Gorum (Chestnutt Hill, MA: Brook Hill Publishing Company, 1974), 299-315
- 38. A. J. Elliott, G. B. Karney, M. F. X. Gigliotti, & T. M. Pollock, "Issues in Processing By the Liquid-Sn Assisted Directional Solidification Technique," *Superalloys 2004*, ed. K. A. Green, T. M. Pollock, H. Harada, T. E. Howson, R. C. Reed, J. J. Schirra, & S. Walston (Warrendale, PA: The Minerals, Metals & Materials Society, 2004), 421-430
- 39. W. Kurz & D. J. Fisher, "Solute Redistribution," *Fundamentals of Solidification*, ed. (Enfield, NH: Trans Tech Publications, 1998), 117-130
- 40. S. M. Roper, S. H. Davis, & P. W. Voorhees, "An Analysis of Convection in a Mushy Layer With a Deformable Permeable Interface," *J. Fluid Mech*, 596 (2008), 333 352.
- 41. S. M. Roper, S. H. Davis, & P. W. Voorhees, "Convection in a Mushy Zone Forced by Sidewall Heat Lossess," *Metall. Mater. Trans. A*, 38A (5) (2007), 1069 1079.
- 42. M. S. Bhat, D. R. Poirier, & J. C. Heinrich, "Permeability for Cross Flow Through Columnar-Dendritic Alloys," *Metall. Mater. Trans. B*, 26B (1995), 1049-1056.
- 43. D. R. Poirier, "Permeability for Flow of Interdendritic Liquid in Columnar-Dendritic Alloys," *Metallurgical and Materials Transactions B*, 18B (1987), 245-255.

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References

[1] K. Mukai, Z. S. Li and K. C. Mills, Met. Trans. B, vol. 36, pg. 255 (2005).

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- J. Madison, J.E. Spowart, D.J. Rowenhorst and, T.M. Pollock, "Three Dimensional Reconstruction of the Dendritic Structure at the Solid-Liquid Interface in a Ni-Base Single Crystal", JOM, July 2008, in press.
- J. Madison, J. Spowart, K. Thornton and T.M. Pollock "Permeability of Directionally Solidified Dendritic Structures in a Ni-Base Superalloy", Acta Materialia, in preparation.
- J. Madison, M. Asta, P. Voorhees and T.M. Pollock, "Convective Instabilities in a Ternary Ni-Al-W Single Crystal", Acta Materialia, in preparation.